

High-power terahertz radiation from relativistic electrons

G. L. Carr*, Michael C. Martin†, Wayne R. McKinney†, K. Jordan‡,
George R. Neil‡ & G. P. Williams‡

*National Synchrotron Light Source, Brookhaven National Laboratory, Upton, New York 11973, USA

†Advanced Light Source Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

‡Free Electron Laser Facility, Jefferson Laboratory, 12000 Jefferson Avenue, Newport News, Virginia 23606, USA

Terahertz (THz) radiation, which lies in the far-infrared region, is at the interface of electronics and photonics. Narrow-band THz radiation can be produced by free-electron lasers¹ and fast diodes^{2,3}. Broadband THz radiation can be produced by thermal sources and, more recently, by table-top laser-driven sources⁴⁻⁶ and by short electron bunches in accelerators⁷, but so far only with low power. Here we report calculations and measurements that confirm the production of high-power broadband THz radiation from sub-picosecond electron bunches in an accelerator. The average power is nearly 20 watts, several orders of magnitude higher than any existing source, which could enable various new applications. In particular, many materials have distinct absorptive and dispersive properties in this spectral range, so that THz imaging could reveal interesting features. For example, it would be possible to image the distribution of specific proteins or water in tissue, or buried metal layers in semiconductors^{8,9}; the present source would allow full-field, real-time capture of such images. High peak and average power THz sources are also critical in driving new nonlinear phenomena and for pump-probe studies of dynamical properties of materials^{10,11}.

The THz region ($1 \text{ THz} < 33 \text{ cm}^{-1}$ or 4 meV) lies in the far-infrared spectral range where conventional thermal sources are very weak. For example, a blackbody source at 2,000 K provides less than 1 mW per cm^{-1} of spectral power density for a typical spectroscopy application. Whereas narrowband sources have been available using free-electron laser (FEL) technology^{1,12}, a significant advance in broadband THz sources has occurred over the past decade with the advent of coherent THz radiation emission from photocarriers in biased semiconductors. Table-top systems using optical rectification of femtosecond lasers either at high repetition rates⁵ or high peak power⁶ are routinely available.

The present work describes a different process for producing coherent THz radiation by accelerated electrons. Like the method described in ref. 5, the process begins with pulsed laser excitation in GaAs, but makes use of photoemission to produce bunches of free electrons in space. Using the energy-recovered linac (ERL) at the Jefferson Laboratory FEL¹³, very short electron bunches ($\sim 500 \text{ fs}$) are brought to relativistic energies (40 MeV) in a linac and then transversely accelerated by a magnetic field to produce the desired THz emission as synchrotron radiation. This unique accelerator is capable of running with a relatively high average beam current (up to 5 mA). Like the THz emitter described in ref. 5, the electrons experience a common acceleration. If the electron bunch dimensions are small (in particular, the bunch length is less than the wavelength of observation), we again obtain a multiparticle coherent enhancement^{14,15}. Such coherent synchrotron radiation has been observed from electrons accelerated in linacs^{7,16-18}, from compact waveguide FELs¹⁹ and from magnetic undulators¹⁹⁻²¹. Coherent THz radiation has been discussed, and observed from electron bunches in storage rings²²⁻²⁵, but not yet stably enough for use as a light source. Active programmes to study THz radiation from linacs or storage rings are underway at BESSY II and DESY in Germany, and at Brookhaven National Laboratory and Lawrence Berkeley National Laboratory in the USA. In addition, programmes are underway at ENEA-Frascati to generate broadband THz radiation by exploiting the distinctive properties of waveguide FELs which arise when the electron velocity is close to the group velocity of the wave packet²⁶. Some linacs can create very short bunches ($< 1 \text{ ps}$) and produce coherent radiation up to a few THz, but most are limited to repetition rates of a few Hz, so the average power is quite low. The repetition rate for storage rings is of the order of 100 MHz, but the electron bunches are significantly longer ($\sim 100 \text{ ps}$) owing to longitudinal damping through synchrotron radiation emission. Thus the emission is limited to the very low frequency regime (far-infrared), or arises from instabilities that briefly modify the bunch shape.

Our ERL accelerator system overcomes some of the limitations of conventional linacs and storage rings. Electron bunches as short as ~500 fs are produced by the standard technique of energy modulation (chirping) followed by compression in the dispersive region of a magnetic chicane²⁷. The time taken for an electron bunch to pass through the accelerator is less than 1ms; thus longitudinal damping is negligible. But unlike most linacs, our system operates at a very high repetition rate (up to 75 MHz) by using superconducting radio frequency cavities and recovering the energy of the spent electron bunches¹³ so that the average current is orders of magnitude higher than in conventional linacs.

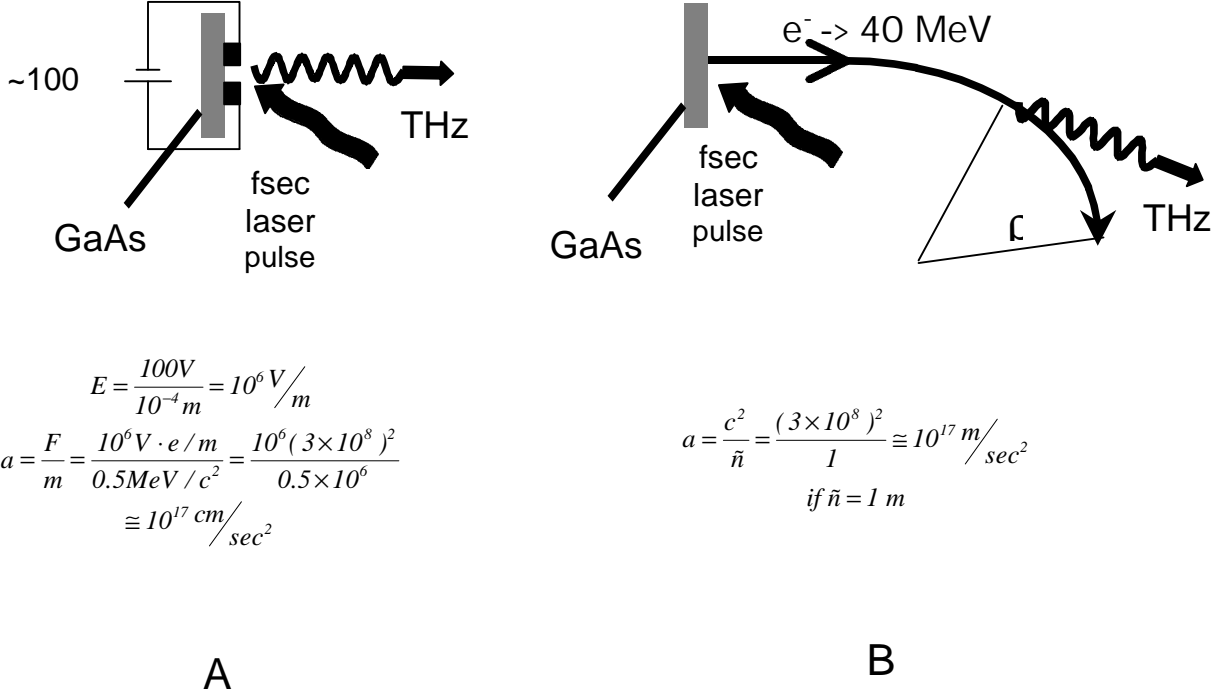


Figure 1 Comparison between coherent THz radiation generated by an 80-MHz conventional laser-driven THz source (a) and the relativistic source described here (b).

We now examine how our system generates THz power many orders of magnitude more efficiently than a more conventional (non-relativistic) THz sources. The diagram in Fig. 1 shows the two processes for comparison. In both cases, a short light pulse from a mode-locked laser strikes a GaAs wafer, generating charge carriers. Thus the number of radiating charges should be comparable (same order of magnitude) for both cases. We can therefore compare the power produced per electron, and use Larmor's formula²⁸ for the radiated power P . In c.g.s. units it takes the form

$$Power = \frac{2e^2 a^2}{3c^3} g^4$$

where e is the charge, a is the acceleration, c the speed of light and g is the ratio of the mass of the electron to its rest mass. With all factors except g the same, we see from equation (1) that for our case the power radiated by a relativistic electron exceeds that from a conventional THz emitter by a factor of $\gamma^4 = 21^4 = 2 \times 10^5$. In practice, the electron energy can be significantly larger, but this simply adds intensity at higher frequencies and leaves the low frequency (THz) intensity essentially unchanged. We mention again that both cases benefit from multiparticle coherent emission, as many radiating charges are contained physically within one period of the emitted THz radiation. Theoretically, the more general expression for the power emitted by an electron bunch, as a function of frequency (ω) and solid angle (Ω), is derived by extending the classical theory of electrodynamics²⁸ for a single electron, to a system of N electrons, thus^{14,15}:

$$\frac{d^2 I}{d\mathbf{w} d\mathbf{W}} = \left[N[1 - f(\mathbf{w})] + N^2 f(\mathbf{w}) \right] \times \frac{e^2 \mathbf{w}^2}{4p^2 c} \left| \int_{-\infty}^{\infty} \hat{n} \times (\bar{\mathbf{b}} \times \hat{n}) e^{i\mathbf{w} \left(t - \frac{\hat{n} \cdot \bar{\mathbf{r}}(t)}{c} \right)} dt \right|^2$$

where b is the ratio of the velocity of the particle bunch to the velocity of light, \hat{n} is a unit vector along the direction of propagation (to the observer), $\mathbf{r}(t)$ is the location of the electron bunch centre, and N is the number of particles in the bunch. The term $N^2 f(\mathbf{q})$ represents the coherent enhancement, and includes the form factor $f(\mathbf{q})$ which is the Fourier transform of the normalized longitudinal particle distribution within the bunch; that is,

$$f(\mathbf{w}) = \left| \int_{-\infty}^{\infty} e^{i\mathbf{w} \hat{n} \cdot \bar{\mathbf{z}} / c} S(z) dz \right|^2$$

where $S(z)$ is the distribution function for particles in the bunch, measured relative to the bunch centre.

A practical solution to the second major term in equation (2) has been presented in ref. 29. For the present calculations (Fig. 2), we assume 40-MeV electron bunches each carrying 100 pC of charge, passing through a 1-m-radius bend at a 37.4-MHz repetition rate. For simplicity, we assume that each bunch has a gaussian particle distribution of width j , yielding a gaussian form factor:

$$f(\mathbf{w}) = e^{-\left(\frac{\mathbf{w} \mathbf{s}}{c}\right)^2} = e^{-4p^2 s^2 \left(\frac{1}{l}\right)^2}$$

where l is the wavelength of the light at frequency q . The bunches are not strictly gaussian in practice, but this approximation is useful for estimating the overall power and spectral content. The electron beam had an r.m.s. width and height of 1 mm. Given a natural emission angle, $1.66(l/r)^{1/3}$ of 0.11 rad at 1 THz, where r is the bending radius, the diffraction-defined source size was of the order of the electron beam size, and the emitted radiation had an extremely high degree of transverse spatial coherence. This allows for interferometry by a simple form of wavefront division³⁰.

In our experiments using the ERL THz source, the electrons were generated using the frequency-doubled output of a Nd:YLF laser (model Antares, made by Coherent) operating at, or a sub-multiple of, 74.8 MHz, and with an average power of a few watts. Light of wavelength 530 nm was incident on a negative electron affinity Cscoated GaAs cathode. The resulting photoelectrons were accelerated using a d.c. voltage of 300 kV into a superconducting linac, and accelerated to an energy of 40 MeV. Although the electrons are initially emitted from the cathode with a pulse length of ~40 ps fullwidth at half-maximum, they become tightly bunched in the accelerator to pulse lengths less than 1 ps. After passing through the accelerator system, the electrons are decelerated in the same linac to an energy of 10 MeV before reaching the beam dump, thus recovering most of the beam energy. This energy recovery allows average current of up to 5 mA and electron bunches containing up to 135 pC, using an r.f. system nominally capable of accelerating only 1.1 mA beam current.

The ERL THz radiation was extracted from a dipole magnet of 1 m bending radius immediately before the FEL cavity, the latter being unimportant for these experiments. For the total power measurements, the radiation left the accelerator vacuum chamber through a 10-mm-aperture diamond window subtending an angle of 20 × 20 mrad relative to the source point. The emerging beam was focused onto a calibrated LiTaO₃ pyroelectric detector, calibrated with equipment traceable to NIST. This detector had a nearly flat response (J25, Molelectron) out to THz wavelengths owing to a black organic coating, and a nominal responsivity of 8.83 V J⁻¹ (±2%).

The spectral content of the ERL THz radiation was analysed using a rapid-scan Michelson interferometer (Nexus 670, Nicolet) with a silicon beamsplitter. The light was detected using a 4.2 K bolometer (Infrared Laboratories) with a 2 mm × 2 mm boron-doped Si composite element, fed from a 12-mm-diameter f/4 Winston cone. It was fitted with a black polyethylene filter to ensure no radiation above 600 cm⁻¹ was

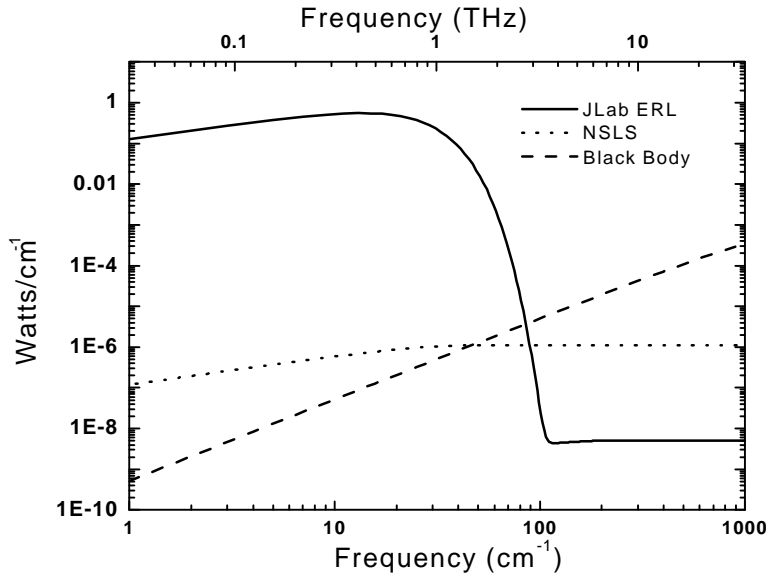


Figure 2 Calculations of the average power emitted by a thermal source at 2,000 K (dashed line), the NSLS VUV ring at Brookhaven National Laboratory (dotted line), and the Jefferson Laboratory (JLab) ERL (solid line).

detected. The diamond window on the accelerator was replaced by a larger crystal-quartz window to increase the energy collection to 60×60 mrad. A spherical mirror of 80 cm focal length produced a 48-mm-diameter collimated beam compatible with the interferometer optics. A switching mirror allowed a remote choice of source, namely the THz energy from the accelerator, or a $T \sim 1,300$ K thermal reference source (see below).

For the spectroscopy experiments, the analysis and detection system did not have sufficient dynamic range to cover the seven decades in power difference between the two sources. But as mentioned earlier, the ERL THz source could be run at a precisely defined lower repetition rate. In this way we could reduce the average power without changing the spectral content. We chose to make measurements at 584 kHz, instead of 37.4 MHz, and at a charge per bunch of 34 pC instead of 100 pC, thereby reducing the ERL THz power by a factor of approximately 550. We have another reference point for determining the absolute power, as we were able to switch sources from the ERL THz emission port to a 1,300 K thermal source (the spectrometer's standard 'globar' source). This allowed us to measure the relative power using the same spectrometer and detection system. At a frequency of 12 cm^{-1} we obtained a ratio of intensity from the ERL THz source to that of the globar of 2×10^4 . To compare with the calculation, we multiply the results for the THz source by the reduction factor of 550, as discussed earlier. This implies a measured advantage of the ERL THz source over the globar of 10^7 . The calculation predicts an enhancement of 10^7 . The data are shown in Fig. 3, and the result affirms the large ERL THz power. The level of agreement is somewhat surprising, as our simple arguments have ignored diffraction and detection efficiency. In fact, owing to uncertainties in the absorbance of the detector coating in the THz region, the reported data place a lower bound on the power measurement.

One additional property of super-radiant emission from electrons is the dependence of the intensity on the square of the number of particles per bunch from equation (2). In Fig. 4 we plot the integrated intensity as a function of bunch charge, which shows good agreement with the theoretical N^2 curve.

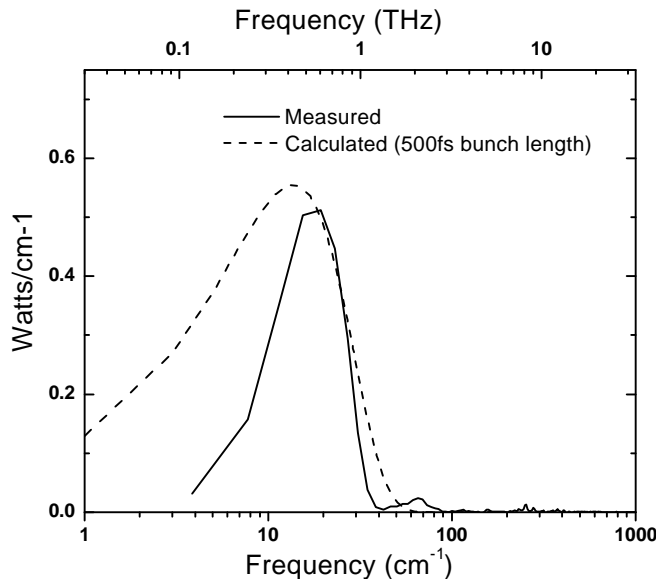


Figure 3 Comparison between measured (solid line) and calculated (dashed line) THz spectral intensity. We have scaled the data to fit the theory on the basis of the absolute power measurements. The spectral onset of the super-radiant enhancement on the high-frequency side is clearly seen, with the shape matching the theoretical prediction. Note that there is a severe discrepancy on the lower-frequency side owing to diffraction effects. This can be understood in the following way. At 10 cm^{-1} and with an $f/17$ beam, the diffraction-limited source size is 17 mm, almost the same as the extraction optics. At 1 cm^{-1} , the diffraction-limited source size would, at 170 mm, be more than 3 times larger than the vacuum chamber containing the electron beam. Note also the additional peak at 60 cm^{-1} , which we attribute to the non-gaussian nature of the electron bunch.

Finally, we measured the polarization of the emitted THz radiation. The intensity ratio for the horizontal to vertical polarization components is 3 for synchrotron radiation in the long-wavelength limit. This assumes full collection of the emitted radiation. We note that the dominant intensity is near 30 cm^{-1} , which has a natural opening angle of 86 mrad. As the emission pattern is ‘clipped’ by the 60-mrad collection optics, the calculated ratio is expected to be higher, approaching a value of 6. Using a wire-grid polarizer placed between the Michelson modulator and the detector, we measured a ratio of 5 and consider this to be good agreement.

We have produced broadband, high-brightness, THz radiation with close to 1 W per cm^{-1} of average spectral power density into the diffraction limit, and peak spectral power densities about 10^4 times higher than this. However, one area of concern remains—the question of timing jitter and current fluctuations, and their effect on coherent detection and signal to noise ratio. As energy-recovery linac THz sources are being considered for other applications, some of which involve timing, it is important to evaluate timing jitter and current fluctuations. We have made preliminary measurements using a frequency analyser, and plan further detailed studies.

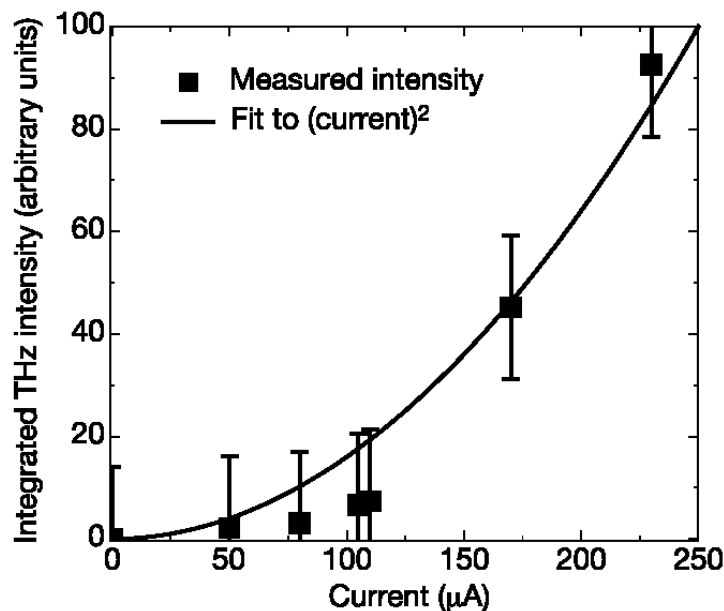


Figure 4 Measured THz intensity as a function of beam current (square symbols), showing the quadratic dependence expected for coherent emission (solid line). We note that in our experiments we were able to observe considerable changes in spectral weight depending on operating conditions, and we were able to enhance certain spectral regions in a controlled way via the machine parameters. Thus the electron bunch distributions were not purely gaussian. This accounts for the large error bars.

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Principal investigator: Michael C. Martin, Advanced Light Source Division, Lawrence Berkeley National Laboratory. Email: MCMartin@lbl.gov. Telephone: 510-495-2231.